

## Lecture 2 - August 27, 2009

## I. chemical equilibrium

## A. mass action law

1. for the reaction:  $aA + bB \rightleftharpoons cC + dD$

a. 
$$\frac{[C]^c [D]^d}{[A]^a [B]^b} = K = \text{an equilibrium constant}$$

2. concentrations are actually divided by their standard states  
 a. equilibrium constants are unitless  
 b. concentration of solutes in moles/L  
 c. concentrations of gases in bars  
 d. concentrations of pure solids, liquids, and solvents are = 1
3.  $K$  is dependent on  $T$  and  $I$

B.  $K$  and  $\Delta G$ 

1. recall:  $\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ$   
 a. if  $\Delta G^\circ < 0$ , the reaction is spontaneous at  $T$   
 b. if  $\Delta G^\circ > 0$ , the reaction is not spontaneous at  $T$
2. can be related to  $\Delta G^\circ$ :

a. 
$$K = e^{-\Delta G^\circ / RT}$$

3. if  $\Delta G^\circ < 0$ ,  $K > 1$   
 4. if  $\Delta G^\circ > 0$ ,  $K < 1$

## C. Le Châtelier's Principle

1. If equilibrium is disturbed by changes in concentrations, temperature, or pressure, the reaction will shift concentrations to return to equilibrium
2. Example:  $\text{Co}(\text{H}_2\text{O})_6^{2+} + 4\text{Cl}^- \rightleftharpoons \text{CoCl}_4^{2-} + 6\text{H}_2\text{O}$   $\Delta H > 0$   
 a.  $\text{Co}(\text{H}_2\text{O})_6^{2+}$  is pink and  $\text{CoCl}_4^{2-}$  is blue  
 b. because  $\Delta H > 0$ , reaction is endothermic, uses heat as it proceeds  
 c. Heat + reactants  $\rightleftharpoons$  products  
 d. add heat, and reaction shift to the right, turns blue
3. temperature affects  $K$   
 a. 
$$K = e^{-\Delta G^\circ / RT}$$
  
 b. 
$$K = e^{-\Delta H^\circ / RT} \cdot e^{\Delta S^\circ / R}$$
  
 i. 1<sup>st</sup> term increases with increasing  $T$   
 ii. 2<sup>nd</sup> term is  $T$  independent  
 c. If  $\Delta H > 0$ ,  $K$  increases with increasing  $T$   
 d. If  $\Delta H < 0$ ,  $K$  decreases with increasing  $T$

## Lecture 2 - August 27, 2009

4. pressure and volume affects equilibrium, if gases are present
- Example:  $\text{N}_2\text{O}_4(\text{g}) \rightleftharpoons 2\text{NO}_2(\text{g}) \quad \Delta H > 0$ 
    - 1 mole of gas converted to 2 moles of gas
    - sudden increase in P
      - increases T, reaction shifts to the right
      - as it cools, shifts to the left, farther than starting position
  - P and V do not change K, simply shift the equilibrium position of the reaction
- D. Equilibrium and Rate
- equilibrium can be defined as the point in a reaction where the forward and reverse rates of reaction are equal
  - K only tells you the thermodynamically-predicted position of the reaction
  - many reactions are slow to reach equilibrium, some never do
  - catalysts
    - a catalyst increases the rate of a reaction
    - provides an alternative, faster pathway from reactants to products
    - does not change the energy difference between the two
    - does not change K or the  $\Delta G^\circ$  for the reaction, only the rate at which equilibrium is reached
- E. Solubility product
- $K_{\text{sp}}$
  - the equilibrium constant for a reaction in which a solid is in equilibrium with its dissolved ions
  - Example mercurous chloride:  $\text{Hg}_2\text{Cl}_2(\text{s})$ ,  $K_{\text{sp}} = 1.2 \times 10^{-18}$ 
    - $\text{Hg}_2\text{Cl}_2(\text{s}) \rightleftharpoons \text{Hg}_2^{2+}(\text{aq}) + 2\text{Cl}^-(\text{aq})$
    - $$K_{\text{sp}} = \frac{[\text{Hg}_2^{2+}(\text{aq})][\text{Cl}^-(\text{aq})]^2}{[\text{Hg}_2\text{Cl}_2(\text{s})]} = [\text{Hg}_2^{2+}(\text{aq})][\text{Cl}^-(\text{aq})]^2 = 1.2 \times 10^{-18}$$
- F. Complex formation
- Many cations and anions react form complex ions
  - The formation of these ions has an equilibrium constant
  - Multiple complexes often form in stepwise fashion
  - Example:  $\text{Pb}^{2+}$  and  $\text{Cl}^-$ 
    - $\text{Pb}^{2+}(\text{aq}) + \text{I}^-(\text{aq}) \rightleftharpoons \text{PbI}^+(\text{aq}) \quad K_1$
    - $\text{PbI}^+(\text{aq}) + \text{I}^-(\text{aq}) \rightleftharpoons \text{PbI}_2(\text{aq}) \quad K_2$
    - $\text{PbI}_2(\text{aq}) + \text{I}^-(\text{aq}) \rightleftharpoons \text{PbI}_3^-(\text{aq}) \quad K_3$
    - can also be written in a cumulative manner
      - $\text{Pb}^{2+}(\text{aq}) + 2\text{I}^-(\text{aq}) \rightleftharpoons \text{PbI}_2(\text{aq}) \quad \beta_2$
      - $\text{Pb}^{2+}(\text{aq}) + 3\text{I}^-(\text{aq}) \rightleftharpoons \text{PbI}_3^-(\text{aq}) \quad \beta_3$
      - $\beta_n = K_1 K_2 K_3 \dots K_n$
  - Often exists in equilibrium with a solid
    - $\text{PbI}_2(\text{s}) \rightleftharpoons \text{Pb}^{2+}(\text{aq}) + 2\text{I}^-(\text{aq}) \quad K_{\text{sp}}$
    - all of the equilibria must be satisfied simultaneously

## Lecture 2 - August 27, 2009

## G. Acids and bases

1. Many compounds can exchange a proton ( $H^+$ )
2. acids increase the  $[H^+]$  in solution
3. bases decrease the  $[H^+]$  in solution, increase the  $[OH^-]$  in solution
4. acids are proton donors, bases are proton acceptors
5. water undergoes autoprotolysis:
  - a.  $H_2O + H_2O \rightleftharpoons H_3O^+ + OH^-$  or  $H_2O \rightleftharpoons H^+ + OH^-$
  - b.  $K_w = [H^+][OH^-] = 1.0 \times 10^{-14}$
  - c. this equilibrium occurs in all aqueous solutions!
  - d. acidity
  - e.  $pH = -\log[H^+]$
  - f.  $pOH = -\log[OH^-]$
  - g.  $pH + pOH = 14$
  - h. strong acids and bases - dissociate completely, no K
6. weak acids
  - a. only partially dissociate
  - b. Example: acetic acid,  $CH_3COOH$
  - c.  $CH_3COOH \rightleftharpoons CH_3COO^- + H^+ \quad K_a$
  - d. 
$$K_a = \frac{[CH_3COO^-][H^+]}{[CH_3COOH]} = 1.75 \times 10^{-5} \quad (just \ an \ equil. \ constant)$$
  - e.  $-\log K_a = pK_a$
  - f. 
$$pH = pK_a + \log \frac{[A^-]}{[HA]} \quad (can \ you \ derive \ this?)$$
  - g. pH vs.  $pK_a$ 
    - i.  $pH < pK_a, [HA] > [A^-]$
    - ii.  $pH > pK_a, [HA] < [A^-]$
    - iii.  $pH = pK_a, [HA] = [A^-]$